

5.1 - Review of Linear Systems

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Unit 4: Systems of Equations & Linear Inequalities

Topic	Assignment
5.1: Review of Linear Systems	Pg. 188 # 1 – 2, 4 – 11 Use Desmos for any question that says to use a graphing calculator
5.2: Solving Nonlinear Systems of Equations	Pg. 195 # 1 – 3, 5 – 8 Use Desmos for any question that says to use a graphing calculator
5.3: Graphing Linear Inequalities in Two Variables	Pg. 205 # 1 – 7 Use Desmos for any question that says to use a graphing calculator
5.4: Solving Systems of Linear Inequalities	Pg. 214 # 1 – 8 Use Desmos for any question that says to use a graphing calculator
5.5: Determining an Optimal Solution	Pg. 221 # 1 – 9
5.6: Modelling & Linear Programming	Pg. 230 # 1 – 7 Use Desmos for any question that says to use a graphing calculator

Recall that a linear equation is an equation that has a degree of one (ie. the variable in the equation is raised only to the power of one).

You've mostly seen linear equations in the following two forms:

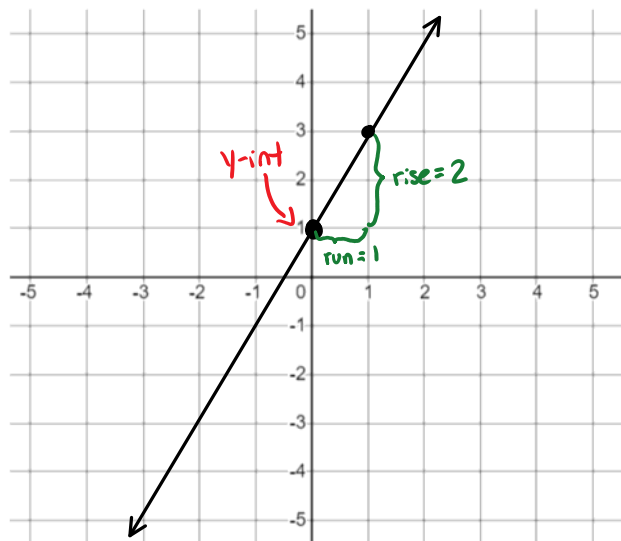
$Ax + By + C = 0$ "General Form" $\left\{ \begin{array}{l} A, B, C \text{ are integers} \\ A \text{ is positive} \end{array} \right.$ ex: $2x - 3y + 4 = 0$

$y = mx + b$ "Slope-Intercept Form" $\left\{ \begin{array}{l} m = \text{slope } \left(\frac{\text{rise}}{\text{run}} \right) \\ b = \text{y-intercept.} \end{array} \right.$
 ex: $y = 2x - 4$

Example

Graph the linear equation $y = 2x + 1$

$\hookrightarrow y = mx + b$
 $m = 2 \rightsquigarrow \text{slope} = \frac{2}{1}$ (rise = 2, run = 1)
 $b = 1 \rightsquigarrow \text{y-int}$



Graphing equations in general form is a little harder. You have two options:

Method 1: Convert to Slope-Intercept Form

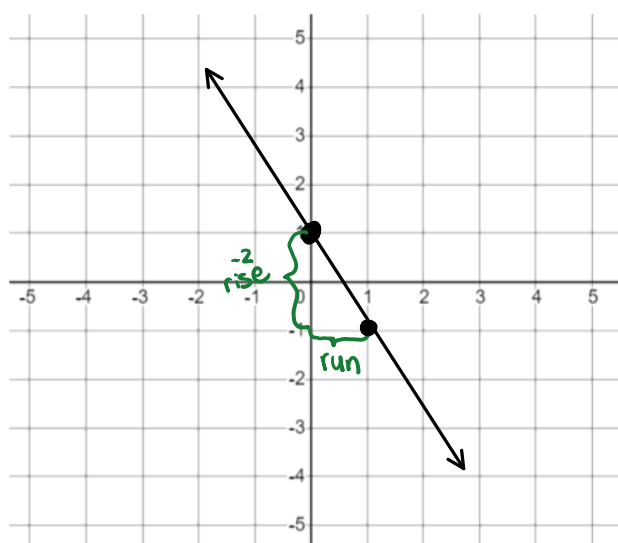
You want to isolate for the dependent variable (usually “y”) and simplify. This will leave you in slope-intercept form, then you can graph as normal.

Example

Graph the equation $4x + 2y - 2 = 0$

$$\begin{aligned}
 4x + 2y - 2 &= 0 \\
 4x + 2y &= 2 \\
 2y &= -4x + 2 \\
 y &= -\frac{4}{2}x + \frac{2}{2} \\
 y &= -2x + 1
 \end{aligned}$$

$y = mx + b$
 $m = -2 = \frac{-2}{1}$
 $b = 1$



Method 2: Determine the x and y-Intercepts and Connect Them

Remember,

x-intercepts occur when $y = 0$

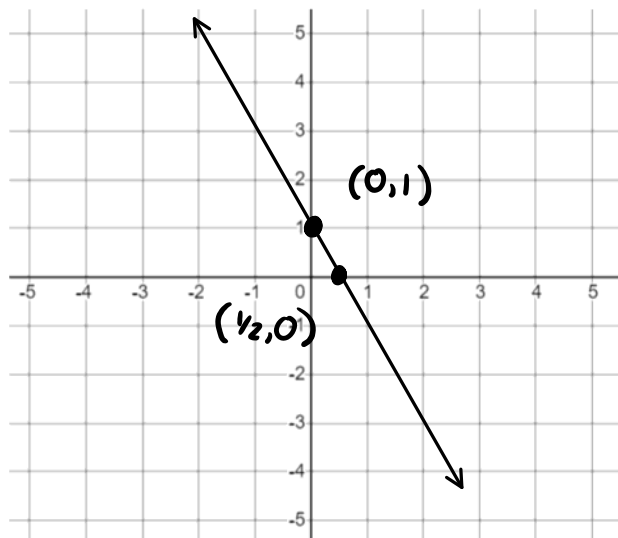
y-intercepts occur when $x = 0$

So, we can substitute $y = 0$ and $x = 0$ to determine the corresponding intercepts and connect them with a line, and then extend the line.

Example

Graph the equation $4x + 2y - 2 = 0$

<p><u>x-int</u> when $y=0$ $4x+2y-2=0$ $4(x)+2(0)-2=0$ $4x-2=0$ $4x=2$ $x=\frac{2}{4}=\frac{1}{2}$ $\therefore (\frac{1}{2}, 0)$</p>	}	<p><u>y-int</u> when $x=0$... $4x+2y-2=0$ $4(0)+2y-2=0$ $2y-2=0$ $2y=2$ $y=\frac{2}{2}=1$ $\therefore (0, 1)$</p>
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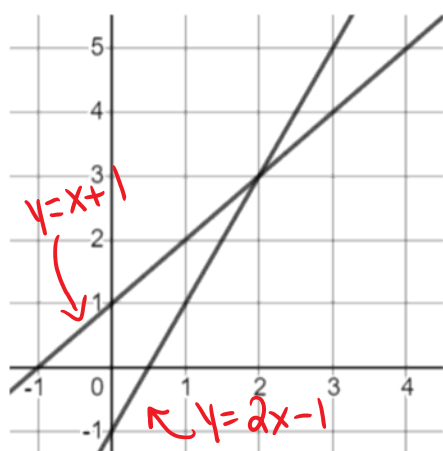


Recall from math 10 the concept of a **system of linear equations**.

In math, a “system” of equations is when 2 or more equations are compared at the same time.

A system of linear equations is when all the equations in the system are linear.

We are said to have “solved” the system when we find points (ie. x and y coordinates) that satisfy the system. Graphically, these points occur where the lines overlap.



Here, I've graphed two linear equations:

$y = 2x - 1$ (the one with y-int of -1)
 $y = x + 1$ (the one with the y-int of 1)

As we can see, even if we extended these lines out to infinity, they would cross only at one point.

In this example, that point is (2, 3). We say that point is the solution to this system of linear equations.

ie. $x = 2, y = 3$

Since we know how to graph lines, we can graph them and see where they intersect, or if we have access to a graphing calculator (such as Desmos) we can graph them there, and see where they intersect.

Example

Solve the following system of equations first without a calculator, then verify your answer with a calculator:

$$\begin{aligned}
 &6x - 3y - 3 = 0 \\
 &y = 9x - 1 \\
 &\hookrightarrow m = \frac{9}{1} \\
 &\rightarrow 6x - 3y - 3 = 0 \\
 &-3y = -6x + 3 \\
 &y = 2x - 1 \\
 &\hookrightarrow m = \frac{2}{1}
 \end{aligned}$$

